# Large- $Q_T$ W-boson production at the Tevatron<sup>1</sup>

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#### Abstract

The production of W bosons at large transverse momentum at the Tevatron is dominated by soft-gluon corrections. In this talk we present a calculation of these corrections at next-to-next-to-leading order. The corrections enhance the transverse momentum distribution of the W while reducing the scale dependence.

<sup>&</sup>lt;sup>1</sup>Presented at DPF04, Riverside, California, August 26-31, 2004.

#### 1 Introduction

W hadroproduction is useful in estimates of backgrounds to new physics (such as Higgs production). The transverse momentum,  $Q_T$ , distribution of the W falls rapidly by several orders of magnitude as  $Q_T$  increases.

Full next-to-leading order (NLO) results for W hadroproduction at large  $Q_T$  have been available for some time [1, 2]. At lowest order the partonic channels involved are  $q(p_a) + g(p_b) \longrightarrow W(Q) + q(p_c)$  and  $q(p_a) + \bar{q}(p_b) \longrightarrow W(Q) + g(p_c)$ . We define  $s = (p_a + p_b)^2$ ,  $t = (p_a - Q)^2$ ,  $u = (p_b - Q)^2$  and  $s_2 = s + t + u - Q^2$ . At threshold, i.e. when we have just enough energy to produce a W with a certain  $Q_T$ ,  $s_2 \to 0$ .

The large- $Q_T$  distribution is enhanced by soft-gluon corrections, which are dominant near threshold. These corrections are of the form  $\mathcal{D}_l(s_2) \equiv [\ln^l(s_2/Q_T^2)/s_2]_+$ . For the order  $\alpha_s^n$  corrections  $l \leq 2n-1$ . At NLO in  $\alpha_s$ , we have terms with  $\mathcal{D}_1(s_2)$  and  $\mathcal{D}_0(s_2)$  logarithms, as well as  $\delta(s_2)$  terms that involve the virtual corrections.

At next-to-next-to-leading order (NNLO) in  $\alpha_s$ , we have terms with  $\mathcal{D}_3(s_2)$ ,  $\mathcal{D}_2(s_2)$ ,  $\mathcal{D}_1(s_2)$ , and  $\mathcal{D}_0(s_2)$  logarithms, as well as  $\delta(s_2)$  terms for the virtual corrections. Thus, at NNLO, the leading logs (LL) are  $\mathcal{D}_3(s_2)$ , the next-to-leading logs (NLL) are  $\mathcal{D}_2(s_2)$ , the next-to-next-to-leading logs (NNLL) are  $\mathcal{D}_0(s_2)$ .

We can formally resum these soft logarithms to all orders in  $\alpha_s$  [3, 4, 5]. This has been done explicitly for W production in Ref. [6]. However, for numerical results here we expand the resummed formula to NNLO to avoid using prescriptions for the resummed cross section [7].

A unified approach and a master formula for calculating these soft logarithms at NNLO for any process has been presented in Ref. [8]. It has been applied to W production in Ref. [9].

## 2 W production with large $Q_T$ at the Tevatron

We now present our numerical results for large- $Q_T$  W-boson production [9] at the Fermilab Tevatron.

The  $Q_T$  distribution is shown in Fig. 1 at Tevatron Run I, with  $\sqrt{S}=1.8$  TeV. In the left frame we show the differential distribution  $d\sigma/dQ_T^2$  at Born (lowest order), NLO, and NNLO, all with scale  $\mu=Q_T$ , while in the right frame we show a plot of the scale dependence at  $Q_T=80$  GeV. For the NNLO corrections we show both NNLL and NNNLL results. The NNLL results are complete while in the NNNLL results we have included the dominant NNNLL terms (more two-loop calculations are needed for an exact NNNLL calculation [10]). Throughout we have used the MRST2002 NNLO parton densities [11]. We see that the NNLO corrections are not very large but they significantly diminish the factorization/renormalization scale dependence of the cross section.

In Fig. 2 we show similar results for Tevatron Run II, with  $\sqrt{S} = 1.96$  TeV. In the left frame we plot  $d\sigma/dQ_T^2$  with  $\mu = Q_T$ , while in the right frame we show results at  $\mu = Q_T/2$  and  $2Q_T$ . Again, the reduction of the scale dependence at NNLO is evident: the two NNLO curves are on top of each other. Finally, we note that similar results have been derived for the related

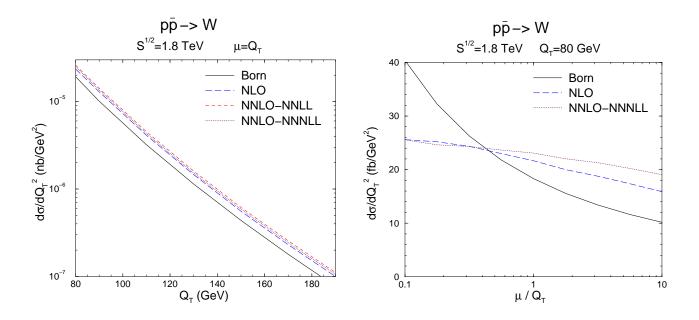


Figure 1: W-boson production at large  $Q_T$  at  $\sqrt{S} = 1.8$  TeV.

process of direct photon production [12].

## Acknowledgments

We thank Richard Gonsalves for help with the NLO corrections. The research of N.K. has been supported by a Marie Curie Fellowship of the European Community program "Improving Human Research Potential" under contract no. HPMF-CT-2001-01221. The work of A.S.V. was supported by an Alexander von Humboldt Postdoctoral Fellowship.

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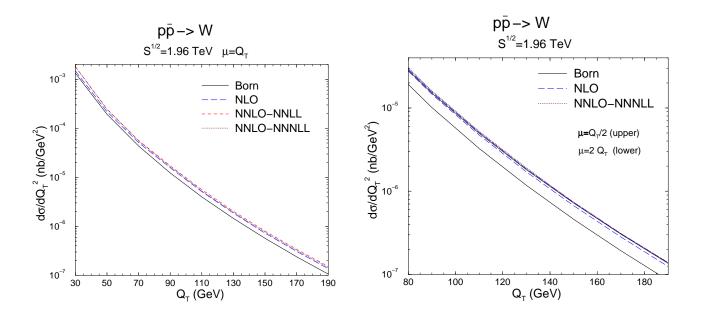


Figure 2: W-boson production at large  $Q_T$  at  $\sqrt{S} = 1.96$  TeV.

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